Enhanced Screening in Chemically Functionalized Graphene

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Resonant scatterers such as hydrogen adatoms can strongly enhance the low energy density of states in graphene. Here, we study the impact of these impurities on the electronic screening. We find a two-faced behavior: Kubo formula calculations reveal an increased dielectric function \( \varepsilon \) upon creation of midgap states but no metallic divergence of the static \( \varepsilon \) at small momentum transfer \( q \to 0 \). This bad metal behavior manifests also in the dynamic polarization function and can be directly measured by means of electron energy loss spectroscopy. A new length scale \( l_c \) beyond which screening is suppressed emerges, which we identify with the Anderson localization length.

Electronic screening presents a central problem in the physics of graphene and strongly affects electron transport as well as effects of electron-electron interactions in this material. First, external perturbations like charged impurities in the graphene substrate can be screened by the graphene electrons and the resulting scattering rate becomes inversely proportional to the squared effective dielectric constant \( \varepsilon \) of graphene \([1,2]\). Second, electron-electron interactions are known to renormalize the charge carrier velocity in graphene near the Dirac point \([3,4]\) and an excitonic instability can be realized depending on \( \varepsilon \) \([5]\).

In reality, graphene samples are subject to disorder, which can alter \( \varepsilon \) significantly. Single impurities can, for instance, lead to high energy plasmon poles of \( \varepsilon \) \([6]\). Most notably, impurities such as hydrogen adatoms can lead to pronounced resonances in the density of states near the Dirac point and related impurity bands can largely increase the low energy density of states (DOS) for impurity concentrations on the order of a few percent or less \([2,7,8,10]\). At high impurity coverages, however, graphene can turn into an insulating material such as graphane \([9,12]\) or fluorographene \([13]\) with band gaps on the order of some eV \([14]\) and thus vanishing DOS at low energies. Regarding the screening of electric fields in graphene it is unclear whether chemical functionalization with species like hydrogen metallizes graphene or rather turns it into an insulator. The answer to question is complicated by the special physics of Anderson localization in this material: The chiral symmetry has been shown to suppress Anderson localization in charge neutral graphene even in presence of strong local impurities \([15,16]\). Away from the neutrality point, however, hydrogen adatoms can lead to Anderson localization \([17]\).

In this letter, we study electronic screening in graphene with resonant scatterers by means of numerically exact Kubo formula calculations \([18,19]\). The dielectric function \( \varepsilon(q, \omega) \) and the dynamic polarization function \( P(q, \omega) \) are discussed as function of momentum transfer \( q \) and frequency \( \omega \). As the central result, we find that resonant impurities turn graphene into a bad metal: Screening in graphene becomes indeed enhanced by chemical functionalization, as the static dielectric function \( \varepsilon(q, \omega = 0) = \varepsilon(q) \) exceeds the pristine graphene value of \( \varepsilon \approx 4.93 \). Below a critical length scale \( l_c \), we find metallic behavior: \( \varepsilon(q) \sim q^{-1} \) for \( q > q_c = 1/l_c \). However, \( \varepsilon(q) \) exhibits a maximum at \( q \sim q_c \) and decreases with \( q \) for \( q < q_c \). Chemically functionalized graphene thus provides metallic screening only at length scales below \( l_c \). We further find bad metal characteristics in the dynamic polarization function and in \( -\text{Im} \varepsilon(q, \omega) \) which can be measured by means of electron energy loss spectroscopy (EELS). By comparing to Green function calculations which neglect vertex corrections, we show that the bad metal behavior is not due to redistribution of single particle spectral weight but due to quantum interference processes. \( l_c \) is identified with the Anderson localization length.

To describe graphene functionalized with chemical species like hydrogen or organic groups, we consider the Hamiltonian \( H = H_{gr} + H_{imp} \). \( H_{gr} = -t \sum_{\langle i,j \rangle} (a_i^\dagger b_j + h.c.) \) is nearest-neighbor tight-binding Hamiltonian of graphene, where \( a_i^\dagger, b_i \) create (annihilates) an electron on sublattice A (B) and \( t = 2.7 eV \) is the nearest neighbor hopping parameter. The adsorbates are taken into account through the Hamiltonian \( H_{imp} = \varepsilon_d \sum_i (d_i^\dagger d_i + V \sum_j (d_j^\dagger c_i + h.c.)) \), where the parameters \( V = 2t, \varepsilon_d = -t/16 \) for hydrogen have been determined by density functional theory (DFT) calculations \([11]\). These impurities lead to resonances in the spectrum of graphene and to the formation of an impurity band, which is energetically very close to the Dirac point.
Recently these impurity states have been observed experimentally by means of scanning tunneling microscopy (STM) \cite{11} and photoemission spectroscopy \cite{20}.

The dynamical polarization function can be obtained from the Kubo formula \cite{23} as

\[ \Pi(q, \omega) = \frac{i}{A} \int_0^\infty d\tau e^{i\omega\tau} \langle \{ \rho(q, \tau) - \rho(-q, 0) \} \rangle, \tag{1} \]

where \( A \) denotes the area of the unit cell, \( \rho(q) = \sum_i c_i^\dagger c_i \exp(iq \cdot r_i) \) is the density operator, and the average is taken over the canonical ensemble. For the case of a single-particle Hamiltonian Eq. (1) can be calculated by means of the Chebyshev polynomial method \cite{12, 13, 14}. The screening of electric fields is determined by the dielectric function \( \varepsilon(q, \omega) \). In the random phase approximation (RPA) it reads \( \varepsilon(q, \omega) = 1 - V(q)\Pi(q, \omega) \), where \( V(q) = 2\pi e^2/q \) is the Fourier component of the Coulomb interaction in two dimensions.

We start with analyzing the static dielectric function (Fig. 1) obtained from our Kubo formula calculations. For pristine graphene, the RPA static dielectric function \( \varepsilon_{G}(q) = 4.93 \) is a constant \cite{24}, which is also found in our calculations. In the presence of hydrogen impurities, one may expect that the screening is highly enhanced due to the emergence of midgap states in the vicinity of the neutrality point and the correspondingly increased density of states around the Fermi level. Indeed, this expectation holds for impurity concentrations up to \( n_i \lesssim 20\% \) and the \( \mathbf{q} \)-vectors \( (q \geq 0.05/a, a \) is carbon-carbon distance) accessible in our simulations \cite{23}. However, the shape of the \( \varepsilon(q) \)-curves does not show purely metallic behavior (i.e. \( \varepsilon(q) \sim q^{-1} \)), as might be expected from the non-zero density of states at the Fermi level: We find \( \varepsilon(q) \sim q^{-1} \) but only for \( q > q_c \), with impurity concentration dependent \( q_c \). \( \varepsilon(q) \) exhibits a maximum at \( q \sim q_c \) and decreases for \( q < q_c \). Electronic screening in graphene is thus enhanced by hydrogen functionalization but fully metallic screening is found only at length scales below \( l_c \sim 1/q_c \).

To understand the origin of this effect, we analyze the static polarization function (\( \Pi(q, \omega = 0) \equiv \Pi(q) \), Fig. 2) obtained from the Kubo formula calculations and compare to the results obtained from evaluating a bubble diagram,

\[ \Pi(q, i\omega_n) = \frac{1}{A\beta} \sum_{\mathbf{k}, \mathbf{n}'} \text{Tr} G(\mathbf{k}, i\omega_n')G(\mathbf{k} + q, i\omega_n + i\omega_n'). \tag{2} \]

Here, \( G(\mathbf{k}, i\omega_n) = (i\omega_n + \mu - v_F(\sigma \cdot \mathbf{k}) - \Sigma(i\omega_n))^{-1} \) is the Green function of graphene with Fermi velocity \( v_F = 3at/2 \) in presence of strong local impurities, which are accounted for by the self-energy \( \Sigma(i\omega_n) = n_iT(i\omega_n) \). In the limit of strong impurity potentials, the \( T \)-matrix entering the self-energy reads \( T(i\omega_n) = -1/G_{\text{loc}}(i\omega_n) \), where \( G_{\text{loc}}(i\omega_n) \) is the local Green function of pristine graphene. This formalism accounts for spectral weight redistribution on a single particle level. The only approximation of Eq. (2) is that it neglects vertex corrections which describe quantum interference effects like Anderson localization.

While both approaches yield the similar \( \Pi(q) \) for larger
evaluated for \( \mu \) adatoms at concentration \( n \). The deviation of fusion coefficients quantitatively, we calculated electronic conductivities long wavelength screening near the neutrality point quantum interference effect involving the hydrogen induced midgap the regime of Anderson localization \([26]\). To corroborate the sample. The spots where the quasi-eigenstates are energy range of the midgap impurity states do not extend through the entire system but are localized in distinct regions of impurities. Therefore, it is understandable why transport localization lengths evaluated at energies different from the chemical potential in the screening calculations display the same trend as \( l_c \) in Fig. 3. Im \( \Pi(\omega, q) \) contains energy resolved information on processes contributing to the electrostatic screening and is closely related to the electron energy loss function \(-\text{Im}(1/\varepsilon(q, \omega))\), which can be measured by EELS. In normal metals we have \( \text{Im} \Pi(\omega, q) \sim \omega/q \), while band insulators show \( \text{Im} \Pi(\omega, q) = 0 \) for energies \( \omega \) less than the band gap. Undoped graphene \( (\mu = 0) \) lies between these cases: Here, only inter-band transitions are allowed, which leads to a peak at \( \omega = v_F q \) in the spectrum of \( \text{Im} \Pi(\omega, q) \). Below
Figure 4. (Color online) Dynamical polarization function of graphene at chemical potential ($\mu = 0$) with (a) different concentrations of impurities and the same wave vector $q = 0.15a^*$ as well as (b) with different wave vectors for the same concentration of impurities. (c) Electron energy loss function $-\text{Im}(1/\varepsilon(q,\omega))$ of graphene with adsorbed hydrogen impurities at concentrations between $n_i = 0$ and $n_i = 2\%$ with fixed $q = 0.15a^{-1}$. There is impurity induced EELS intensity at energies $\omega < v_F q$, which is energetically forbidden in pristine graphene. (d) $-\text{Im}(1/\varepsilon(q,\omega))$ in the low energy region for different momentum transfers $q$ at fixed impurity concentration $n_i = 0.5\%$.

In conclusion, we have studied electronic screening in graphene with resonant impurities. We show that the quasilocalized states in the vicinity of neutrality point lead to "bad metal" behavior. Resonant impurities make screening more efficient and render graphene metallic but only up to a certain critical length scale $l_c$. This scale is determined by Anderson localization and corresponds to the inter-impurity spacing. As a consequence, scattering of the graphene electrons by external potentials, which vary on length scales which are large compared to the interatomic spacing but smaller than $l_c$, is suppressed due to screening by the midgap states.

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Due to limitations of present computer power, it is numerically too expensive to get reliable values of the polarization function for wave vectors $q < 0.05/a$.


A normal metal yields $\text{Re} \Pi(q \to 0, \omega = 0) = \kappa$ and $\text{Im} \Pi(q \to 0, \omega \to 0) = \xi \omega/q$ with constants $\kappa$ and $\xi$. In RPA, we have $\varepsilon(q, \omega) = 1 - (2\pi\varepsilon^2/q)\Pi(q, \omega)$ and consequently $\text{Re} \varepsilon(q, \omega) \gg \text{Im} \varepsilon(q, \omega)$ if $\kappa q \gg \xi \omega$. At sufficiently small frequencies it is thus $-\text{Im} 1/\varepsilon(q, \omega) = \text{Im} \varepsilon(q, \omega)/(\text{Re} \varepsilon(q, \omega))^2 \sim \omega q^0$. 